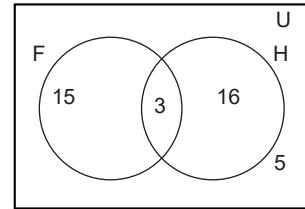


Worksheet

1. Fill in the blanks.
 - a. If $A = \{\text{letters of the word INDIA}\}$ and $B = \{\text{letters of the word HINDI}\}$, then $A \cap B = \underline{\hspace{2cm}}$.
 - b. If $U = \{x : x \in \mathbf{W}, x < 5\}$ and $A = \{x : x \in \mathbf{N}, 1 < x < 5\}$, then $A' = \underline{\hspace{2cm}}$.
 - c. If $A = \{2, 3, 5, 7\}$ and $B = \{1, 4, 2, 5\}$, then $A - B = \underline{\hspace{2cm}}$.
 - d. If $n(A) = 10$ and $n(A \cup B) = 17$, then $n(B - A) = \underline{\hspace{2cm}}$.
 - e. If $n(A - B) = 2$, $n(B - A) = 3$ and $n(A \cup B) = 7$, then $n(A \cap B) = \underline{\hspace{2cm}}$.
2. State if the following statements are true or false.
 - a. $A \cup (B \cup C) = A \cap (B \cup C)$
 - b. $A' \cap B' = (A \cup B)'$
 - c. $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$
 - d. $(A \cap B)' = A' \cap B'$
 - e. If $A = \{\text{factors of } 35\}$ and $B = \{\text{factors of } 20\}$, then $n(A \cap B) = 1$.
3. If $A = \{3, 4, 5, 6\}$, $B = \{1, 2, 6, 8\}$ and $C = \{1, 2, 3, 4, 5\}$, then find
 - a. $A \cup B$
 - b. $A \cup C$
 - c. $B \cup C$
 - d. $A \cup (B \cup C)$
 - e. $A \cap B$
 - f. $B \cap C$
 - g. $C \cap A$
 - h. $A \cap (B \cap C)$
 - i. $(A \cap B) \cup C$
4. Find the union, intersection and difference ($A - B$) and ($B - A$) of the following pair of sets.
 - a. $A = \{x : -5 < x < 5, x \in \mathbf{Z}\}$ and $B = \{x : -2 < x < 5, x \in \mathbf{Z}\}$
 - b. $A = \{x : 4 < x < 7, x \in \mathbf{N}\}$ and $B = \{x : 0 < x < 7, x \in \mathbf{W}\}$
5. If $U = \{1, 2, 3, 4, \dots, 10\}$, $A = \{2, 4, 6, 8\}$, $B = \{1, 2, 3, 5, 7\}$ and $C = \{1, 2, 3, 5, 7, 8\}$, then find
 - a. A'
 - b. B'
 - c. C'
 - d. $A \cup B$
 - e. $(A \cup C)$
 - f. $(A \cup B) \cup C$
 - g. $A - B$
 - h. $(B - C)$
6. If $A = \{x, y, z, t\}$, $B = \{z, t, u\}$ and $C = \{x, y, u, v\}$, then show that
 - a. $(A \cup B) \cup C = A \cup (B \cup C)$
 - b. $(A \cap B) \cap C = A \cap (B \cap C)$
7. If $U = \{1, 2, 3, 4, 5, 6\}$, $A = \{2, 3, 4, 5\}$ and $B = \{1, 2, 3, 5\}$, then verify
 - a. $(A \cup B)' = A' \cap B'$
 - b. $(A \cap B)' = A' \cup B'$
8. If $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$, $A = \{1, 2, 3, 5, 6, 7, 8\}$ and $B = \{1, 3, 4, 6, 7, 8, 9\}$. Illustrate the following on a Venn diagram.
 - a. $A \cap B$
 - b. $A - B$
 - c. B'
9. If $A = \{3, 6, 9, 12\}$, $B = \{2, 4, 6, 8, 10, 12\}$ and $C = \{6, 12, 18\}$, then show that
 - a. $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$
 - b. $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
10. If $n(A) = 14$, $n(B) = 12$ and $n(A \cap B) = 6$, then find
 - a. $n(A \cup B)$
 - b. $n(A - B)$
11. If $n(A) = 15$, $n(B) = 10$ and $n(A \cup B) = 20$, find
 - a. $n(A - B)$
 - b. $n(B - A)$

12. Represent the following using Venn diagram:
 $U = \{a, b, c, d, e, f\}$, $A = \{a, b, c\}$, $B = \{b, c, e\}$
13. The given Venn diagram illustrates the following information:
 U = number of students in a class
 F = number of students who play football
 H = number of students who play hockey
Find:
a. the number of students who play football.
b. the number of students in the class.
c. the number of students who play football and hockey.
d. the number of students who play football or hockey.
14. If X and Y are two sets such that $X \cup Y$ has 45 elements, X has 24 elements and Y has 26 elements, how many elements does $X \cap Y$ have?
15. In a group of 20 girls who like coffee or chips, 8 like chips but not coffee and 12 like chips, find
a. how many girls like both chips and coffee?
b. how many girls like coffee but not chips?
16. In a club, 20 members like hot or cold coffee, 12 members like hot coffee, 6 members like hot and cold coffee both. How many members in the club like cold coffee, if all the members like atleast one drink?



Answers to Worksheet

- | | | | | |
|--|---------------------------------|------------------------------|------------------|----------|
| 1. a. $\{I, N, D\}$ | b. $\{0, 1\}$ | c. $\{3, 7\}$ | d. 7 | e. 12 |
| 2. a. False | b. True | c. True | d. False | e. False |
| 3. a. $\{1, 2, 3, 4, 5, 6, 8\}$ | b. $\{1, 2, 3, 4, 5, 6\}$ | c. $\{1, 2, 3, 4, 5, 6, 8\}$ | | |
| d. $\{1, 2, 3, 4, 5, 6, 8\}$ | e. $\{6\}$ | f. $\{1, 2\}$ | g. $\{3, 4, 5\}$ | |
| h. \emptyset | i. $\{1, 2, 3, 4, 5, 6\}$ | | | |
| 4. a. $A \cup B = \{x : x \in \mathbb{Z}, -5 < x < 5\}$, $A \cap B = \{x : x \in \mathbb{Z}, -2 < x < 5\}$,
$A - B = \{x : x \in \mathbb{Z}, -5 < x < -1\}$; $B - A = \emptyset$ | | | | |
| b. $A \cup B = \{x : x \in \mathbb{N}, 0 < x < 7\}$, $A \cap B = \{x : x \in \mathbb{N}, 4 < x < 7\}$,
$A - B = \emptyset$, $B - A = \{x : x \in \mathbb{W}, 0 < x < 5\}$ | | | | |
| 5. a. $\{1, 3, 5, 7, 9, 10\}$ | b. $\{4, 6, 8, 9, 10\}$ | | | |
| c. $\{4, 6, 9, 10\}$ | d. $\{1, 2, 3, 4, 5, 6, 7, 8\}$ | | | |
| e. $\{1, 2, 3, 4, 5, 6, 7, 8\}$ | f. $\{1, 2, 3, 4, 5, 6, 7, 8\}$ | | | |
| g. $\{4, 6, 8\}$ | h. \emptyset | | | |
| 10. a. 20 | b. 8 | 11. a. 10 | b. 5 | |
| 13. a. 18 | b. 39 | c. 3 | d. 34 | |
| 14. 5 | 15. a. 4 | b. 8 | c. 3 | 16. 14 |